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by

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Vertical differentiation, schedule delay and entry deterrence: Low cost vs. full service airlines[§]

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Abstract

We consider a market with a full-service (*FS*) carrier (the incumbent) and a low-cost (*LC*) carrier (the potential entrant). If the *LC* carrier enters the market, airlines compete in ticket prices and frequency with vertically differentiated products. The higher the frequency, the lower passenger's generalized price. Thus, more frequency allows airlines to increase ticket prices without losing demand. In this context, we show that the incumbent may increase the frequency offered in order to deter the *LC* carrier entry. We show that if the airport capacity is low enough the *LC* carrier entry can be easily blocked or deterred. However, if the airport capacity is sufficiently high, the *LC* carrier entry must be accommodated.

Keywords: Low-cost (*LC*) carriers, full-service (*FS*) carriers, schedule delay, entry deterrence

JEL Classification: L93, L12, L15

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1. Introduction

Low-cost (*LC*) carriers have acquired a significant market share in the last decades and it seems that it will continue growing in the future (Dobruszkes, 2006). Full-service (*FS*) carriers have been affected for this new model of airline business¹ and the competition between these two types of airlines is commonly observed.²

FS carriers and *LC* carriers differ in their quality and their costs, and thus, in the ticket prices charged to passengers.³ Thus, several authors argue that *LC* and *FS* carriers compete in differentiated products (see, for example, Gillen and Morrison, 2003; Barbot, 2004, 2006, 2008; Fu *et al.*, 2011; or Hazledine, 2011).

FS carriers and *LC* carriers not only differ in their quality and fare but they also differ in their frequency. *FS* carriers usually offer more frequent flights than *LC* carriers (Gillen and Morrison, 2003) and for this reason passengers can select a flight departure time that is closer to their preferred one. Passengers will be better off the smaller the difference between the real and the preferred departure time, and this difference is the so-called schedule delay.⁴ There are some papers in the literature that consider airlines that compete in fare and frequency (see, for example, Yetiskul *et al.*, 2005; Brueckner

¹ See, for example, Doganis (2001), Franke (2004), or O'Connell and Williams (2005) for historical notes of changes that affected the *FS* carrier model.

² See, for example, Pels (2008) for an analysis of the process of airline deregulation and its importance in the "low-cost airline revolution". This author also explains the effects of low-cost revolution in airline network.

³ Franke (2004) argues that *LC* carriers can deliver 80% of the service quality with approximately 50% of the cost of *FS* carriers.

⁴ There are some papers in the literature finding important effects of the scheduling cost (see, for example, Douglas and Miller, 1974; Anderson and Kraus, 1981; Lijesen, 2006; or Hess *et al.*, 2007). In a recent paper, Koster *et al.* (2013) point out that travellers do not only consider arrivals delays, but also face scheduling costs because they arrive too early or too late at their destination. Earlier studies that consider travel delay variability for travellers going to the airport are Koster *et al.* (2011) and Tam *et al.* (2008).

and Flores-Fillol, 2007; or Yetiskul and Kanafani, 2010). However, none of these papers consider competition in fares and frequency between airlines that offer flights with different qualities.⁵

In this paper, we consider a vertically differentiated product model as the one used by Shaked-Sutton (1982). However, we depart from Shaked-Sutton's model in the following. On the one hand, contrary to Shaked-Sutton (1982), we assume non-linear cost functions for airlines, capturing the economies from operating larger aircraft (Brueckner, 2004; Brueckner and Flores-Fillol, 2007). Moreover, we assume that *LC* carriers have lower operating costs per flight than *FS* carriers. On the other hand, we assume that passengers' demand depends on airlines' generalized price, which is defined as the sum of the ticket price and the value of the total time spent by the consumer in the travel (which includes not only access, egress and in-vehicle time but also the schedule delay cost). In particular, we consider a market with a *FS* carrier (the incumbent) and a *LC* carrier (the potential entrant) that may enter the market. If the *LC* carrier enters the market, airlines compete in ticket prices and frequency with vertically differentiated products. In this context, we show that the incumbent may increase the frequency offered in order to deter the *LC* carrier entry.

We follow Dixit (1980)'s approach in which an incumbent decides whether to accommodate entry or to deter it through excess capacity. However, there are substantial differences. On the one hand, in our model the higher the frequency (capacity), the lower the passenger's generalized price. Thus, more frequency allows airlines to increase ticket prices without losing demand. On the other hand, contrary to Dixit (1980), we do not need to assume any fixed cost of entry for the *LC* carrier.

We show that, even if the airport has no capacity constraints, if the airport capacity is low enough the *LC* carrier entry can be blocked. Moreover, we show that the *FS* carrier

⁵ We consider competition between *LC* and *FS* carriers in the same airport. It is also possible the competition between both type of carriers serving different airports (see, for example, Pels *et al.* 2000; 2003; 2009)

optimally deters the *LC* carrier entry for intermediate values of the airport capacity. Finally, if the airport capacity is high enough, the *LC* carrier entry cannot be blocked or deterred and, thus, it must be accommodated.

Previous research on entry deterrence in the air transport market is mostly devoted to analyse the role of fare as an entry deterrence strategy (see, for example, Windle and Dresner, 1995, 1999; Goolsbee and Syverson, 2008; Huse and Oliveira, 2010; Tan, 2011; or Aydemir, 2012), or the effects on hub and spoke networks (see, for example, Oum *et al.*, 1995) and code share alliances (see, for example, Lin, 2005, 2008). However, few papers analyse the effects of capacity (frequency) on entry deterrence. One exception is Morrison (2004) that highlights that capacity expansion by an incumbent airline may represent a credible threat for potential entrants since some fixed inputs need not be permanently assigned to a particular city pair. Empirical evidence of the use of frequency as an entry deterrence strategy in air transport markets is still scarce. However, we would like to highlight two papers. On the one hand, Goolsbee and Syverson (2008) find weak evidence to support that the incumbents expand capacity as an entry deterrence strategy in air transport markets. On the other hand, Ng *et al.* (1999) interview 36 service firms to explore their practices of capacity usage. Their study shows that 25 per cent of service firms interviewed expand their capacity to deter entrants. Among them, they find an airline that expanded the capacity on certain routes to ensure that others carriers do not enter the market. The results of this paper that relate the use of frequency as an entry deterrence strategy and the level of airport capacity may explain the divergences between the findings of Goolsbee and Syverson (2008) and Ng *et al.* (1999).

Finally, we have to highlight that the European regulation of slots is based on the so-called “Grandfather rights”, that is, the rights of the incumbent airlines. Because of it, if an airline uses a slot in the previous season, it will be entitled to continue using it in the

next period.⁶ With this regulation, an airline could use the frequency as an entry deterrence strategy and the potential competitor cannot do anything to avoid it.

The rest of the paper is organized as follows. In Section 2 we explain the main assumptions of the model. Section 3 analyses the competition in prices with vertically differentiated products. In Section 4 we describe how the *LC* carrier decides whether to enter or not the market. Section 5 analyses the *FS* carrier optimal choice of frequency in order to deter or accommodate the *LC* carrier entry. Finally, Section 6 concludes.

2. Model setup

Suppose a market which is operated just by one full-service (*FS*) carrier, the incumbent. However, there is one low-cost carrier (*LC*) that may enter the market. *FS* and *LC* carriers offer flights with different levels of quality. We assume that the *FS* carrier has a first mover advantage and can decide the frequency it will offer before the *LC* carrier decides or not to enter the market. Thus, if the *LC* carrier decides to enter the market, it must decide its frequency and carriers will compete in prices with vertically differentiated products.

Following Brueckner (2004) and Brueckner and Flores-Fillol (2007), we can define each flight operating cost by:

$$c_k = \theta_k + \tau_k s_k, \quad (1)$$

⁶ The basic legislation of Grandfather Rights is Council Regulation 95/93 on common rules for the allocation of slots at Community airports. It introduces a new principle: “use it or lose it” (also known as the “80/20 rule”). With this principle, an airline could lose its slots if it has not used it the 80% of the time. Moreover, non-used slots and newly created ones must go to a pool, with 50% of them being reserved for new entrants (Betancor and de Rus, 2003). Also there have been several amendments to this regulation (for example, for exceptional circumstances like the actual economic crisis).

where θ_k is a fixed cost for airline k , s_k denotes the number of seats in airline k and τ_k is the marginal cost per seat in airline k , with $k = LC, FS$. Assuming a load factor of a 100%, the connection between frequency (f_k) and traffic (q_k) is given by the equation $q_k = f_k s_k$, that is, the total traffic is equal to the number of flights times the number of seats per flight. We suppose that the *LC* carrier has lower costs than the *FS* carrier, both in the fixed part of the cost of each flight and the marginal cost per seat of each flight, that is, $\theta_{LC} < \theta_{FS}$ and $\tau_{LC} < \tau_{FS}$.⁷ We do not assume any fixed cost of entry for the *LC* carrier.⁸

We assume that there is a continuum of consumers who are identical in tastes but they differ in income. The income (m) is assumed to be uniformly distributed between the interval $[a, b]$, with $0 < a \leq m \leq b$. Consumers have a unitary demand, that is, they buy (or not) only one ticket from one of the two carriers at price p_k .

We denote by H the number of available hours and by f_k the number of flights offered by airline k . The value of the total time spent by the consumer in the travel (T_k) is the sum of the value of the time spent in the trip (which includes access, egress and in-vehicle time), A_k , and the average schedule delay cost ($\delta H / 4f_k$), being δ the cost of each hour of difference between the preferred and the actual departure time. Formally:⁹

⁷ *LC* carriers have lower average cost than *FS* carriers because several reasons: higher seating density, highly daily aircraft utilisation, lower airport charges, minimum cabin crews, lower passenger services (e.g. meals and drinks), e-ticketing, use of secondary airports, minimal station costs (ground staff, check-in, related facilities of the airports,...), etc.

⁸ Fixed cost of entry is a common assumption in the entry deterrence literature. In this paper, we show that even if we do not consider such a fixed entry cost, entry can be blocked or deterred.

⁹ We suppose that consumers' preferred departure times are spaced around the clock. H/f represents the time interval between flights and if consumers' preferred departure time is uniformly distributed around the clock, $H/4f$ is the average time to the nearest flight (Brueckner, 2004). One prior analysis of

$$T_k = A_k + \delta \frac{H}{4f_k}. \quad (2)$$

Thus, we can define the generalized price for the consumer as the sum of the ticket price and the value of the total time spent by the consumer in the travel, that is:

$$G_k = p_k + A_k + \delta \frac{H}{4f_k}. \quad (3)$$

The consumers' utility function is given by $U(m, k, G_k)$, which denotes the utility derived from consuming m units of income and one unit of product k , with a generalized cost of G_k . Formally:

$$U(m, k, G_k) = u_k(m - G_k) = u_k(m - p_k - T_k) = u_k \left[m - \left(p_k + A_k + \delta \frac{H}{4f_k} \right) \right], \quad (4)$$

where u_k denotes the consumer satisfaction when flying with airline k . Since the *LC* carrier has a lower level of quality than the *FS* carrier, we assume that $0 < u_{LC} < u_{FS}$. Thus, a consumer only flies with a *LC* carrier if $G_{LC} < G_{FS}$, that is, if the sum of the price, the value of the time spent in the trip and the schedule delay cost for a *LC* airline is lower than for a *FS* carrier. This is stated in the following lemma.

Lemma 1: *No consumer flies with a LC carrier if $G_{LC} \geq G_{FS}$.*

Lemma 1 states that, even though a *FS* carrier may charge a higher ticket price than the *LC* carrier, if the former manages to offer a frequency high enough to compensate such a higher ticket price, no consumer will fly with a *LC* carrier.

scheduling that incorporates these principles is Panzar (1979). See also Koster and Verhoef (2012) for other references in more general scheduling models.

Let $B_{FS} = u_{FS} / (u_{FS} - u_{LC})$ be the relative utility gain of buying a ticket in a *FS* carrier instead of in a *LC* carrier, that is, it measures how the utility changes when switching from the *LC* to the *FS* carrier. Notice that, since $0 < u_{LC} < u_{FS}$, B_{FS} is strictly higher than zero and higher than one, that is, $B_{FS} > 0$ and $1 - B_{FS} < 0$.

Similarly, we can also define $B_{LC} = u_{LC} / (u_{LC} - u_0)$ as the relative utility gain of buying a ticket in a *LC* carrier, that is, it measures how the utility changes when switching from an outside option to the *LC* carrier, where u_0 is the satisfaction obtained consuming this outside option. The outside option may represent an alternative mode of transport or even not travel at all. We assume that $u_0 < u_{LC}$ and, for the sake of simplicity, we normalize the parameter $u_0 = 0$. Then, without loss of generality, we assume that $B_{LC} = 1$.

First of all, we have to find the so called “indifferent consumer”, that is, we have to find the consumer that is indifferent between flying with a *LC* carrier at a generalized cost G_{LC} or flying with a *FS* carrier at a generalized cost $G_{FS} > G_{LC}$. Formally:

$$U(m, FS, G_{FS}) = U(m, LC, G_{LC}),$$

that is;

$$u_{FS}(m - G_{FS}) = u_{LC}(m - G_{LC}).$$

Thus:

$$m_{FS} = B_{FS}G_{FS} + (1 - B_{FS})G_{LC}, \quad (5)$$

where m_{FS} is the rent for the indifferent consumer between *FS* and *LC* carriers.

Lemma 2: *The consumer that is indifferent between flying with a LC carrier at a generalized cost G_{LC} or flying with a FS carrier at a generalized cost $G_{FS} > G_{LC}$ has a rent $m_{FS} = B_{FS}G_{FS} + (1 - B_{FS})G_{LC}$.*

Similarly, we can find the consumer that is indifferent between travelling with the LC carrier and the outside option:

$$U(m, LC, G_{LC}) = U(m, 0, 0),$$

that is:

$$u_{LC}(m - G_{LC}) = 0.$$

Then:

$$m_{LC} = G_{LC}, \tag{6}$$

where m_{LC} is the rent for the indifferent consumer between LC carrier and the outside option.

Lemma 3: *The consumer that is indifferent between travelling with a LC carrier at a generalized cost G_{LC} or an outside option with $u_0 = 0$ has a rent $m_{LC} = G_{LC}$.*

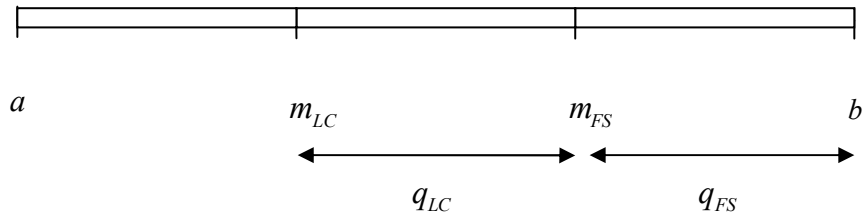
Corollary 1: *In the optimum m_{LC} can never be lower than a since it is always profitable for the LC carrier to choose a generalize price G_{LC} such that at least the consumer with the lowest rent buys a LC ticket.*

Notice that, given that for a consumer to fly with a LC carrier we need $G_{LC} < G_{FS}$, we have that $m_{FS} - m_{LC} = B_{FS}(G_{FS} - G_{LC}) > 0$. So we can state the following corollary:

Corollary 2: *There is always space in this market for the two carriers.*

We have to take into account that the consumer with income $m > m_{FS}$ strictly prefers the *FS* flight at the generalized price G_{FS} to the *LC* flight at the generalized price $G_{LC} < G_{FS}$. Consumers are divided into segments, and these segments correspond with the successive market shares of rival firms, q_{LC} and q_{FS} , as shown in Figure 1.

Figure 1. Indifferent consumer position and market shares



Let us now analyse how the indifferent consumers move in the income space.

Lemma 4: *The indifferent consumer between the LC and FS carrier is moved to the right in the income space if the FS carrier's generalized price increases and is moved to the left if the LC carrier's generalized price decreases.*

Proof: It is straight forward to check the sign of the following derivatives:

$$\frac{\partial m_{FS}}{\partial G_{FS}} > 0, \text{ and } \frac{\partial m_{FS}}{\partial G_{LC}} < 0. \quad \blacksquare$$

In other words, if any part of the generalized price (ticket price, value of the travel time or schedule delay cost) of the *FS* carrier rises, the indifferent consumer will be a person who has more rent to afford a trip with a *FS* carrier. In contrast, if the *LC* carrier's generalized price increases, the indifferent consumer will be a person with less income because, given the higher *LC* carrier's generalized price, the previous one will not be indifferent anymore and will decided to travel with a *FS* carrier.

Lemma 5: *The indifferent consumer between the LC and the outside option is moved to the right in the income space if the LC carrier's generalized price increases.*

Proof: It is straight forward to check the sign of the following derivative: $\frac{\partial m_{LC}}{\partial G_{LC}} > 0$. ■

The intuition behind Lemma 5 is similar to the one of Lemma 4.

Carriers' generalized price depends both on the ticket price and the frequency and, thus, both variables are crucial for the computation of carriers' demand.

The timing of the game is as follows: First, the *FS* carrier decides its frequency (with the corresponding first mover advantage). Second, the *LC* carrier decides whether to enter or not in the market. If the *LC* carrier decides to enter, given the frequency of the *FS* carrier, it must decide the frequency to be offered. In the third stage, companies choose the optimal ticket prices. If the *LC* carrier decided not to enter, the *FS* carrier chooses the optimal price as a monopolist. If the *LC* carrier decided to enter, both the *FS* carrier and the *LC* carrier compete in prices with vertically differentiated products. The game is solved by backward induction.

3. Third Stage: Optimal ticket prices

In the last stage of the model carriers must choose the optimal ticket prices. There are only two possibilities: If the *LC* carrier decides to enter the market, we have a duopoly situation. However, if it is not profitable for the *LC* carrier to enter the market (whatever the reason) the market is served only by the *FS* carrier.

3.1 The duopoly solution

If the *LC* carrier decides to enter the market, the *FS* and *LC* carrier compete in ticket prices with vertically differentiated products. At this stage *FS* and *LC* frequencies are given.

Recall that $q_k = f_k s_k$, with $k = LC, FS$ and $q_{FS} = b - m_{FS}$. Then, the *FS* carrier solves the following maximization program:

$$\begin{aligned} \underset{p_{FS}}{\text{Max}} \pi_{FS} &= p_{FS}(b - m_{FS}) - f_{FS}c_{FS} = p_{FS}(b - m_{FS}) - f_{FS}(\theta_{FS} + \tau_{FS}s_{FS}) = \\ &= (p_{FS} - \tau_{FS})(b - m_{FS}) - f_{FS}\theta_{FS}. \end{aligned} \quad (7)$$

Similarly, recall that $q_{LC} = m_{FS} - m_{LC}$. Thus, the *LC* carrier solves the following maximization program:

$$\underset{p_{LC}}{\text{Max}} \pi_{LC} = (p_{LC} - \tau_{LC})(m_{FS} - m_{LC}) - f_{LC}\theta_{LC}. \quad (8)$$

First order conditions for the above maximization programs are given by:

$$b - m_{FS} - (p_{FS} - \tau_{FS}) \frac{\partial m_{FS}}{\partial p_{FS}} = 0, \quad (9)$$

$$m_{FS} - m_{LC} + (p_{LC} - \tau_{LC}) \left(\frac{\partial m_{FS}}{\partial p_{LC}} - \frac{\partial m_{LC}}{\partial p_{LC}} \right) = 0. \quad (10)$$

That is:

$$b - m_{FS} - (p_{FS} - \tau_{FS})B_{FS} = 0, \quad (11)$$

$$m_{FS} - m_{LC} - (p_{LC} - \tau_{LC})B_{FS} = 0. \quad (12)$$

The solution to these conditions gives us the optimal ticket prices to be charged by the *LC* and *FS* carrier (given the frequencies that have been chosen in the previous stages of the game) in a duopoly situation:

$$p_{FS}^D = \frac{2b + 2B_{FS}\tau_{FS} + (B_{FS} - 1)\tau_{LC} - (1 + B_{FS})T_{FS} + (B_{FS} - 1)T_{LC}}{3B_{FS} + 1}, \quad (13)$$

$$p_{LC}^D = \frac{b + B_{FS}\tau_{FS} + 2B_{FS}\tau_{LC} + B_{FS}T_{FS} - (1 + B_{FS})T_{LC}}{3B_{FS} + 1}. \quad (14)$$

The corresponding duopoly benefits are given by:

$$\pi_{FS}^D = B_{FS} \frac{(-2b + (B_{FS} + 1)\tau_{FS} - (B_{FS} - 1)\tau_{LC} + (1 + B_{FS})T_{FS} - (B_{FS} - 1)T_{LC})^2}{3B_{FS} + 1} - \theta_{FS} f_{FS}, \quad (15)$$

$$\pi_{LC}^D = B_{FS} \frac{(b + B_{FS}\tau_{FS} - (1 + B_{FS})\tau_{LC} + B_{FS}T_{FS} - (1 + B_{FS})T_{LC})^2}{3B_{FS} + 1} - \theta_{LC} f_{LC}. \quad (16)$$

3.2. The monopoly solution

If the *LC* carrier does not enter the market, the *FS* carrier chooses the ticket prices that maximize its profits as a monopolist. Thus, the *FS* carrier solves the following maximization program:

$$\underset{p_{FS}}{\text{Max}} \pi_{FS} = (p_{FS} - \tau_{FS})(b - m_{FS}) - f_{FS}\theta_{FS}, \quad (17)$$

with $m_{FS} = G_{FS}$.

The first order condition of the above maximization program is given by:

$$-2p_{FS} + \tau_{FS} + b - T_{FS} = 0. \quad (18)$$

The optimal ticket price in a monopoly situation is thus given by:

$$p_{FS}^M = \frac{1}{2}(b + \tau_{FS} - T_{FS}). \quad (19)$$

The monopoly *FS* carrier's profits are given by:

$$\pi_{FS}^M = \frac{1}{4}((b - \tau_{FS})^2 + T_{FS}(-2b + 2\tau_{FS} + T_{FS})) - \theta_{FS} f_{FS}. \quad (20)$$

Table 1 summarizes the duopoly and monopoly solutions.

Table 1. The duopoly and monopoly solutions

	Duopoly	Monopoly
Prices	$p_{FS}^D = \frac{2b + 2B_{FS}\tau_{FS} + (B_{FS} - 1)\tau_{LC} - (1 + B_{FS})T_{FS} + (B_{FS} - 1)T_{LC}}{3B_{FS} + 1}$ $p_{LC}^D = \frac{b + B_{FS}\tau_{FS} + 2B_{FS}\tau_{LC} + B_{FS}T_{FS} - (1 + B_{FS})T_{LC}}{3B_{FS} + 1}$	$p_{FS}^M = \frac{1}{2}(b + \tau_{FS} - T_{FS})$
Generalized cost	$G_{FS}^D = \frac{2b + 2B_{FS}\tau_{FS} + (B_{FS} - 1)\tau_{LC} + 2B_{FS}T_{FS} + (B_{FS} - 1)T_{LC}}{3B_{FS} + 1}$ $G_{LC}^D = \frac{b + B_{FS}\tau_{FS} + 2B_{FS}\tau_{LC} + B_{FS}T_{FS} + 2B_{FS}T_{LC}}{3B_{FS} + 1}$	$p_{FS}^M = \frac{1}{2}(b + \tau_{FS} - T_{FS}) + T_{FS}$
Indifferent incomes	$m_{FS}^D = \frac{(B_{FS} + 1)(b + B_{FS}\tau_{FS}) - (B_{FS} - 1)B_{FS}\tau_{LC} + B_{FS}(B_{FS} + 1)T_{FS} - (B_{FS} - 1)B_{FS}T_{LC}}{3B_{FS} + 1}$ $m_{LC}^D = \frac{b + B_{FS}\tau_{FS} + 2B_{FS}\tau_{LC} + B_{FS}T_{FS} + 2B_{FS}T_{LC}}{3B_{FS} + 1}$	$m_{FS}^M = \frac{1}{2}(b + \tau_{FS} - T_{FS}) + T_{FS}$
Profits	$\pi_{FS}^D = B_{FS} \frac{(-2b + (B_{FS} + 1)\tau_{FS} - (B_{FS} - 1)\tau_{LC} + (1 + B_{FS})T_{FS} - (B_{FS} - 1)T_{LC})^2}{3B_{FS} + 1} - \theta_{FS}f_{FS}$ $\pi_{LC}^D = B_{FS} \frac{(b + B_{FS}\tau_{FS} - (1 + B_{FS})\tau_{LC} + B_{FS}T_{FS} - (1 + B_{FS})T_{LC})^2}{3B_{FS} + 1} - \theta_{LC}f_{LC}$	$\pi_{FS}^M = \frac{1}{4}((b - \tau_{FS})^2 + T_{FS}(-2b + 2\tau_{FS} + T_{FS})) - \theta_{FS}f_{FS}$

4. Second Stage: The *LC* carrier's decisions

Given the frequency chosen by the *FS* carrier in the first period, the *LC* carrier must decide whether or not to enter the market. If the *LC* carrier finally decides to enter the market, it must choose the frequency to be offered taking into account the competition in prices that will take place in the next period.

Let f_{FS} be the frequency offered by the *FS* carrier in the first period, which at this stage is given. Let us denote by K the capacity of the airport. Let f_{LC}^* denote the optimal frequency offered by the *LC* carrier if it decides to enter, which is given by:

$$f_{LC}^* = \text{Max}\{0, \text{Min}\{K - f_{FS}, \bar{f}_{LC}\}\}, \quad (21)$$

where \bar{f}_{LC} is the optimal solution of the following maximization program (the duopoly solution):

$$\begin{aligned} \text{Max}_{f_{LC}} \pi_{LC}^D(f_{FS}, f_{LC}) &= \\ &= B_{FS} \frac{\left(b + B_{FS}\tau_{FS} - (1 + B_{FS})\tau_{LC} + B_{FS}T_{FS}(f_{FS}) - (1 + B_{FS})T_{LC}(f_{LC})\right)^2}{3B_{FS} + 1} - \theta_{LC}f_{LC}. \end{aligned} \quad (22)$$

In other words, the *LC* carrier chooses a frequency that depends on the capacity of the airport. If the capacity is not high enough to allow the *LC* carrier to choose its optimal frequency, it must conform to the spare capacity.

Let us denote by $\pi_{LC}^D(f_{FS}, f_{LC}^*)$ the profits obtained by the *LC* carrier if it enters the market. If $0 < K - f_{FS} < \bar{f}_{LC}$, that is, there is no space in the airport in order to allow to *LC* carrier to choose the optimal frequency, then $f_{LC}^* = K - f_{FS}$. Thus, in this case, the lower the airport capacity is, the further is f_{LC}^* from the optimum \bar{f}_{LC} , and the lower $\pi_{LC}^D(f_{FS}, f_{LC}^*)$ is. This is formally stated in the following lemma.

Lemma 6: *If $0 < K - f_{FS} < \bar{f}_{LC}$, then $\partial \pi_{LC}^D(f_{FS}, f_{LC}^*) / \partial K \geq 0$.*

Finally, the *LC* carrier decides to enter the market if the profits it obtains when entering are higher than zero, that is, if $\pi_{LC}^D(f_{FS}, f_{LC}^*) > 0$.

5. First Stage: The *FS* carrier's optimal frequency

Even though Corollary 2 states that there is always space in this market for the two carriers, the *FS* carrier can serve the whole market for two reasons. On the one hand, the entry may be blocked (for example, because the airport capacity may be low enough to allow the presence of only one firm). On the other hand, the *FS* carrier may choose a frequency that deters the *LC* carrier entry. We will analyse all the possibilities in this section.

5.1 Blocked entry

We say that entry is blocked if, even if the *FS* carrier chooses the frequency that maximizes its profits as a monopolist, the *LC* carrier cannot enter the market.

Let us denote by f_{FS}^M the optimal frequency for the *FS* carrier as a monopolist, which is the solution of the following maximization program:

$$\text{Max}_{f_{FS}} \pi_{FS}^M(f_{FS}) = \frac{1}{4} \left((b - \tau_{FS})^2 + T_{FS}(-2b + 2\tau_{FS} + T_{FS}) \right) - \theta_{FS} f_{FS}. \quad (23)$$

If given the monopoly frequency for the *FS* carrier, f_{FS}^M , the *LC* carrier's benefits are negative, then entry is blocked. Denote by f_{LC}^M the frequency offered by the *LC* carrier given the frequency offered by the *FS* carrier as a monopolist, that is:

$$f_{LC}^M = \text{Max} \left\{ 0, \text{Min} \left\{ K - f_{FS}^M, \bar{f}_{LC}^M \right\} \right\}, \quad (24)$$

where \bar{f}_{LC}^M is the solution of the following maximization program:

$$\begin{aligned} \text{Max}_{f_{LC}} \pi_{LC}^D(f_{FS}^M, f_{LC}) &= \\ &= B_{FS} \frac{\left(b + B_{FS} \tau_{FS} - (1 + B_{FS}) \tau_{LC} + B_{FS} T_{FS}(f_{FS}^M) - (1 + B_{FS}) T_{LC}(f_{LC}) \right)^2}{3B_{FS} + 1} - \theta_{LC} f_{LC}. \end{aligned} \quad (25)$$

Thus, the value of \bar{f}_{LC}^M is implicitly defined by the following first order condition:

$$\begin{aligned} -2(1 + B_{FS}) B_{FS} \frac{\left(b + B_{FS} \tau_{FS} - (1 + B_{FS}) \tau_{LC} + B_{FS} T_{FS}(f_{FS}^M) - (1 + B_{FS}) T_{LC}(\bar{f}_{LC}^M) \right)}{3B_{FS} + 1} \frac{\partial T_{LC}}{\partial f_{LC}}(\bar{f}_{LC}^M) \\ - \theta_{LC} = 0. \end{aligned} \quad (26)$$

Proposition 1: Entry is blocked for the LC carrier if and only if $\pi_{LC}^D(f_{FS}^M, f_{LC}^M) \leq 0$. On the contrary, entry cannot be blocked for the LC carrier if $\pi_{LC}^D(f_{FS}^M, f_{LC}^M) > 0$.

Recall that we are assuming that the LC carrier's operating cost per flight is always lower than the FS carrier's and there is no fixed cost of entry for the LC carrier.¹⁰ Moreover, Corollary 2 states that there is always space in this market for the two carriers. However, we will show that the airport capacity may be too low to allow both carriers to operate the market. Thus, the LC carrier entry may be blocked due to capacity restrictions, as it is stated in the following proposition.

Proposition 2: There always exists a critical value for the airport capacity \bar{K} such that if $K \leq \bar{K}$ the entry is blocked for the LC carrier. On the contrary, if $K > \bar{K}$ entry cannot be blocked and, thus, it must be either deterred or accommodated.

Proof: If K is too small in the sense that it is impossible for the LC carrier to reach the optimal frequency, the LC carrier frequency will be either zero or $K - f_{FS}^M$. If $f_{LC}^M = 0$ the proof is trivial. If $f_{LC}^M = K - f_{FS}^M$, the LC carrier's benefits will be given by:

$$\begin{aligned} \pi_{LC}^D(f_{FS}^M, K - f_{FS}^M) &= \\ &= B_{FS} \frac{(b + B_{FS}\tau_{FS} - (1 + B_{FS})\tau_{LC} + B_{FS}T_{FS}(f_{FS}^M) - (1 + B_{FS})T_{LC}(K - f_{FS}^M))^2}{3B_{FS} + 1} - \theta_{LC}(K - f_{FS}^M). \end{aligned}$$

Solving $\pi_{LC}^D(f_{FS}^M, K - f_{FS}^M) = 0$ we can obtain the critical value of the airport capacity \bar{K} .

This completes the proof. ■

¹⁰ Assuming a fixed cost of entry for the LC carrier would reinforce even more our results.

5.2. Entry deterrence versus accommodated entry

Even if the entry cannot be blocked, the *FS* carrier may be interested in deterring the *LC* carrier entry. This means that the *FS* carrier modifies its frequency in order to make the *LC* carrier's profits lower than or equal to zero.

Let us denote by f_{FS}^E the entry deterrence frequency for the *FS* carrier, that is, the frequency that makes the profits for the *LC* carrier in the duopoly equal to zero.

Given f_{FS}^E , the *LC* carrier chooses the frequency f_{LC}^E , that is:

$$f_{LC}^E = \text{Max}\{0, \text{Min}\{K - f_{FS}^E, \bar{f}_{LC}^E\}\}, \quad (27)$$

where the value of \bar{f}_{LC}^E comes from the following first order condition:

$$\begin{aligned} -2(1+B_{FS})B_{FS} \frac{(b+B_{FS}\tau_{FS} - (1+B_{FS})\tau_{LC} + B_{FS}T_{FS}(f_{FS}^E) - (1+B_{FS})T_{LC}(\bar{f}_{LC}^E))}{3B_{FS}+1} \frac{\partial T_{LC}}{\partial f_{LC}}(\bar{f}_{LC}^E) \\ -\theta_{LC} = 0. \end{aligned} \quad (28)$$

The *FS* entry deterrence frequency f_{FS}^E is then implicitly defined by the following equation:

$$\begin{aligned} \pi_{LC}^D(f_{FS}^E, f_{LC}^E) = \\ = B_{FS} \frac{(b+B_{FS}\tau_{FS} - (1+B_{FS})\tau_{LC} + B_{FS}T_{FS}(f_{FS}^E) - (1+B_{FS})T_{LC}(f_{LC}^E))^2}{3B_{FS}+1} - \theta_{LC} f_{LC}^E = 0. \end{aligned} \quad (29)$$

Let us denote by f_{FS}^D the frequency offered by the *FS* carrier if it knows that the *LC* carrier will enter the market and it will face a duopoly situation. Thus, f_{FS}^D is the solution of the following maximization problem:

$$\begin{aligned}
& \text{Max}_{f_{FS}} \pi_{FS}^D(f_{FS}, f_{LC}^D) = \\
& = B_{FS} \frac{\left(-2b + (B_{FS} + 1)\tau_{FS} - (B_{FS} - 1)\tau_{LC} + (1 + B_{FS})T_{FS}(f_{FS}) - (B_{FS} - 1)T_{LC}(f_{LC}^D)\right)^2}{3B_{FS} + 1} - \theta_{FS} f_{FS},
\end{aligned} \tag{30}$$

where $f_{LC}^D = \min\{K - f_{FS}^D, \bar{f}_{LC}^D\}$, and \bar{f}_{LC}^D is implicitly defined by the following first order condition:

$$\begin{aligned}
& -2(1 + B_{FS})B_{FS} \frac{\left(b + B_{FS}\tau_{FS} - (1 + B_{FS})\tau_{LC} + B_{FS}T_{FS}(f_{FS}^D) - (1 + B_{FS})T_{LC}(\bar{f}_{LC}^D)\right)}{3B_{FS} + 1} \frac{\partial T_{LC}}{\partial f_{LC}}(\bar{f}_{LC}^D) \\
& - \theta_{LC} = 0.
\end{aligned} \tag{31}$$

The *FS* carrier will deter the *LC* carrier entry if the profits the former obtains with the frequency f_{FS}^E as a monopolist are higher than the *FS* carrier's profits in a duopoly situation with a frequency f_{FS}^D . Otherwise, entry is accommodated. This is formally stated in the following proposition.

Proposition 3: *If $\pi_{FS}^M(f_{FS}^E, f_{LC}^E) > \pi_{FS}^D(f_{FS}^D, f_{LC}^D)$, the *FS* carrier deters the entry for the *LC* carrier. On the contrary, if $\pi_{FS}^M(f_{FS}^E) \leq \pi_{FS}^D(f_{FS}^D, f_{LC}^D)$ the *LC* carrier entry is accommodated.*

From Proposition 2 we know that if the airport capacity is higher than the critical value \bar{K} , that is $K > \bar{K}$, entry cannot be blocked. However, we can always find a critical value for the airport capacity such that the *LC* carrier entry is deterred. The intuition is that, if the airport capacity is sufficiently close to the critical value \bar{K} , we can always find another critical value $\bar{\bar{K}}$ such that if $\bar{K} < K \leq \bar{\bar{K}}$ it is always profitable for the *FS* carrier to deter the entry. This is formally stated in the following proposition.

Proposition 4: *There always exists a critical value for the airport capacity $\overline{\overline{K}}$ such that if $\overline{K} < K \leq \overline{\overline{K}}$ the entry is deterred for the LC carrier.*

Proof: Suppose that $\overline{K} < K$. From the proof of Proposition 2 we know that if $\overline{K} < K$ entry cannot be blocked. However, we can always find a frequency for the FS carrier, $f_{FS}^{E^*} > f_{FS}^M$, such that $f_{LC}^E = K - f_{FS}^{E^*} > 0$. Then, the LC carrier's benefits will be given by:

$$\pi_{LC}^D(f_{FS}^{E^*}, K - f_{FS}^{E^*}) = \frac{B_{FS} \left((b + B_{FS}\tau_{FS} - (1 + B_{FS})\tau_{LC} + B_{FS}T_{FS}(f_{FS}^{E^*}) - (1 + B_{FS})T_{LC}(K - f_{FS}^{E^*}))^2 \right)}{3B_{FS} + 1} - \theta_{LC}(K - f_{FS}^{E^*}).$$

Solving for $\pi_{LC}^D(f_{FS}^{E^*}, K - f_{FS}^{E^*}) = 0$ we can obtain the critical value of the airport capacity $\overline{\overline{K}}$. We have just guarantee that the LC carrier will not enter if $\overline{K} < K \leq \overline{\overline{K}}$. However, we must also guarantee that there always exist a $\overline{\overline{K}}$ such that if $\overline{K} < K \leq \overline{\overline{K}}$ entry deterrence is profitable for the FS carrier, that is, $\pi_{FS}^M(f_{FS}^{E^*}) > \pi_{FS}^D(f_{FS}^D, f_{LC}^D)$. The latter condition will always hold if $\overline{\overline{K}}$ is sufficiently close to \overline{K} and thus $f_{FS}^{E^*}$ is close enough to f_{FS}^M . This completes the proof. ■

Finally, since we have not considered any fixed cost of entry for the LC carrier, if the airport capacity is high enough, FS carrier will not able to deter or blocked the entry and a duopoly situation will take place. This is formally stated in the following corollary.

Corollary 3: *If the airport capacity is high enough, that is, $K > \overline{\overline{K}}$, the LC carrier entry cannot be blocked or deterred. Thus, the LC carrier entry must be accommodated.*

6. Conclusions

In this paper we analyse a vertically differentiated product market to explain full-service (FS) and low-cost (LC) airlines' competition. We consider that passengers have a preferred departure time and dislike the schedule delay, that is, the difference between

the real and preferred departure time. As the frequency increases, passengers' schedule delay cost decreases and, hence, airlines can charge a higher ticket price without losing demand. In this context, we analyse under which circumstances the *FS* carrier is interested in increasing its frequency in order to deter or accommodate the *LC* carrier entry.

We find that the use of the frequency as an entry deterrence strategy is closely related with the level of airport capacity. We show that the higher the airport capacity is, the more difficult is for the incumbent to deter the *LC* carrier entry and more difficult to have a blocked entry. Although the empirical research to support the use of frequency as an entry deterrence strategy is still scarce in the air transport literature, our results might be used as a justification to explain why *LC* carriers usually operate in airports that are not congested at all.

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